

# Neurons, Lymphatics and Cancer: modelling a dangerous trio



ΕΛΛΗΝΙΚΗ ΔΗΜΟΚΡΑΤΙΑ  
Εθνικόν και Καποδιστριακόν  
Πανεπιστήμιον Αθηνών  
— ΙΔΡΥΘΕΝ ΤΟ 1837 —

## Μαστρογιάννη Μαρία

ΤΡΙΜΕΛΗΣ ΕΠΙΤΡΟΠΗ ΔΙΠΛΩΜΑΤΙΚΗΣ ΕΡΓΑΣΙΑΣ

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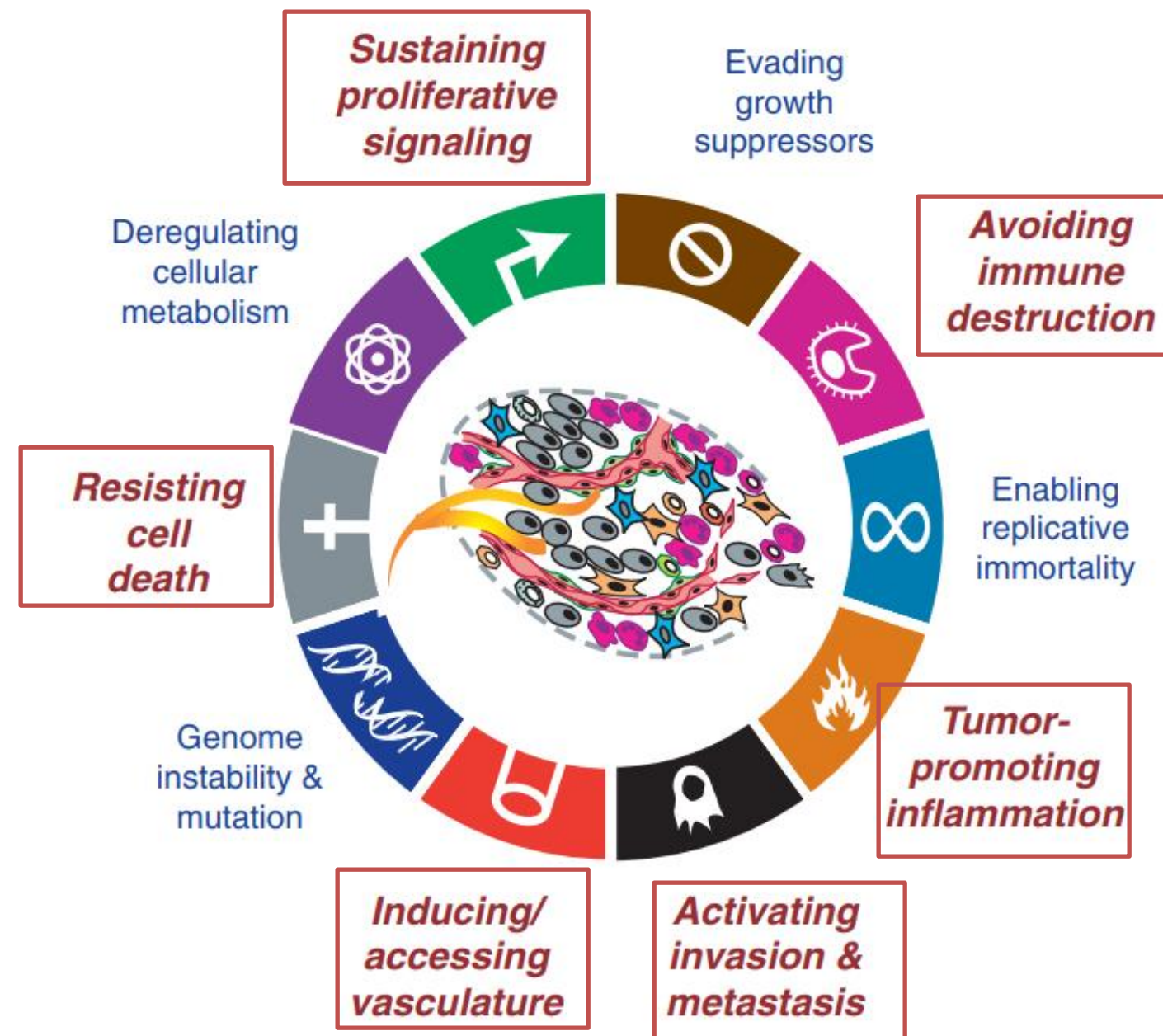
**ΣΥΜΒΟΥΛΟΙ:** Dr. Georgios Lolas & Dr. Arianna Bianchi

# Overview

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- Introduction to the field of Cancer Neuroscience
- The role of Perineural Invasion
- Mathematical modelling of Perineural Invasion (PNI)
- Simulations
- Discussion and future direction

# Cancer Neuroscience



➤ New field of research entitled cancer neuroscience.

➤ Recent evidence indicates that the nervous system plays a central role in cancer pathogenesis<sup>2</sup>.

The nervous system influences six of the fundamental characteristics that make up the core hallmarks<sup>2</sup>.

1) Hanahan, D., & Monje, M. (2023). Cancer hallmarks intersect with neuroscience in the tumor microenvironment. *Cancer Cell*, 41(3), 573-580.

2) Monje, M., Borniger, J. C., D'Silva, N. J., Deneen, B., Dirks, P. B., Fattahi, F., ... & Winkler, F. (2020). Roadmap for the emerging field of cancer neuroscience. *Cell*, 181(2), 219-222.

# Perineural Invasion

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- The ability of tumor cells to proliferate around nerves and to invade them<sup>3</sup>
- Marker of poor prognosis<sup>2</sup>
- Has been reported in a variety<sup>1</sup> of cancers, including colorectal , pancreatic, prostate cancer etc.

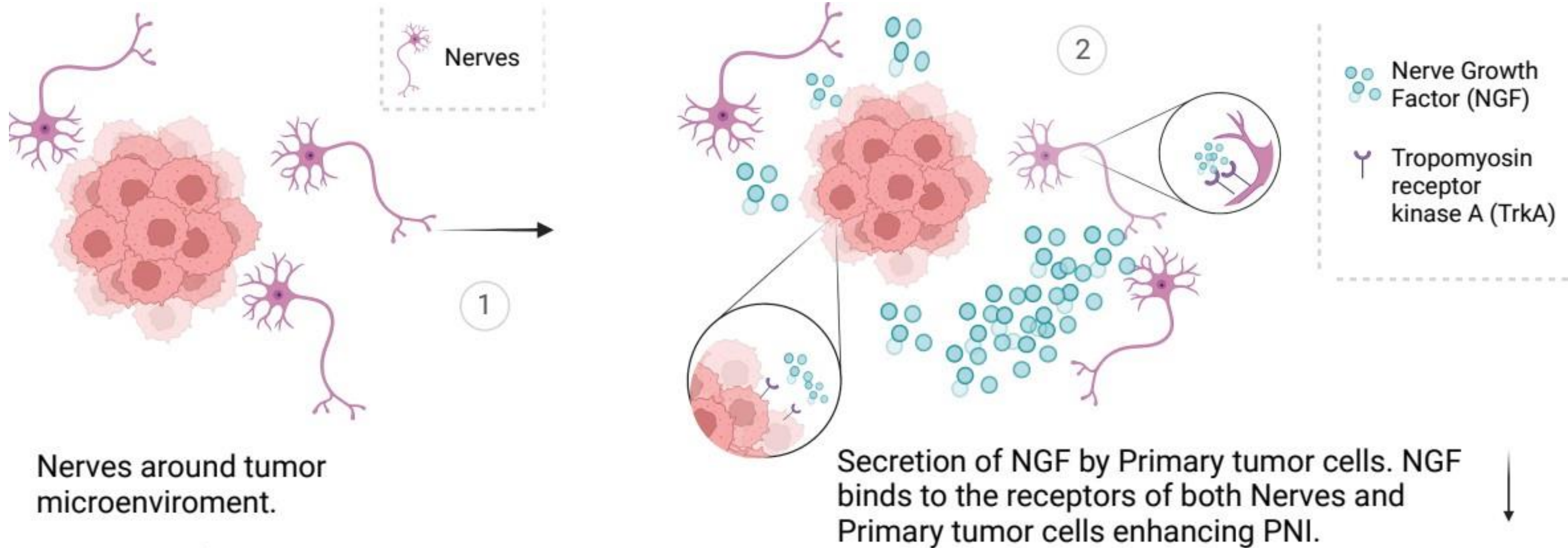
1) Amit, M., Na'Ara, S., & Gil, Z. (2016). Mechanisms of cancer dissemination along nerves. Nature reviews Cancer, 16(6), 399-408

2) Magnon C. Role of the nerves in the tumor microenvironment. Prog Mol Biol Transl Sci. 2015;131:151-175

3) Wang, W., Li, L., Chen, N., Niu, C., Li, Z., Hu, J., & Cui, J. (2020). Nerves in the tumor microenvironment: origin and effects. Frontiers in Cell and Developmental Biology, 8, 601738

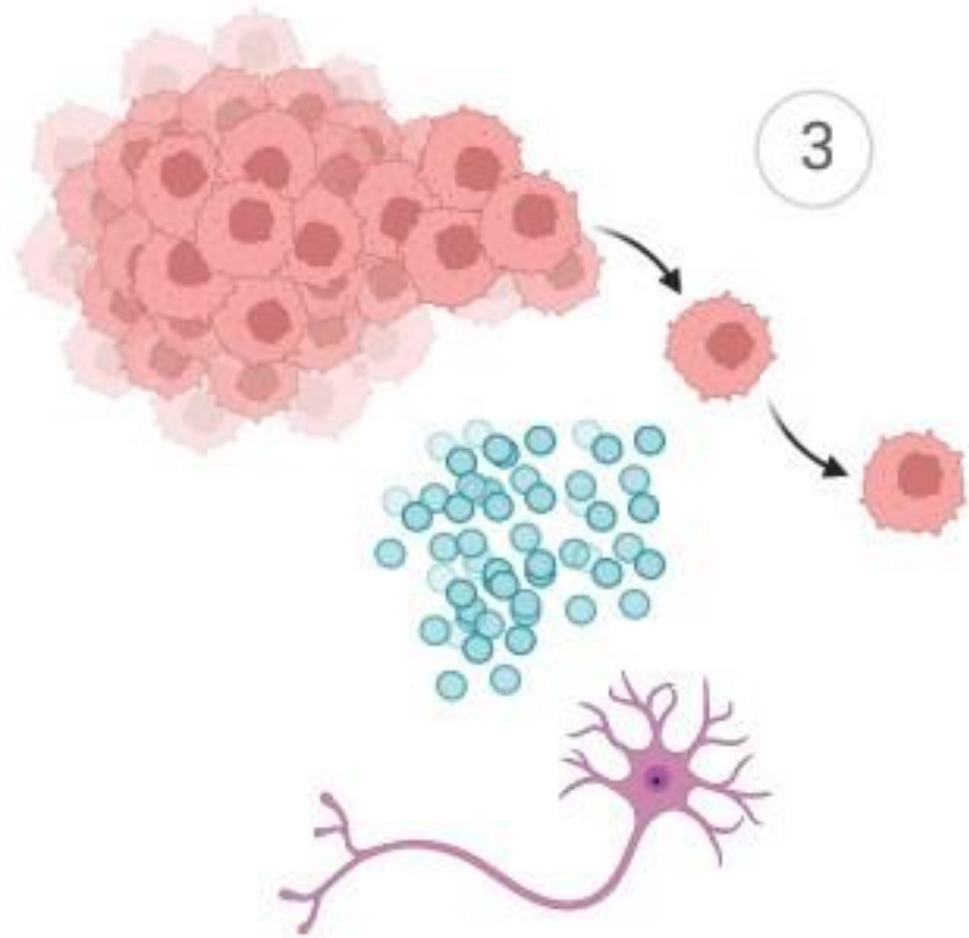


# Mechanism of Perineural Invasion

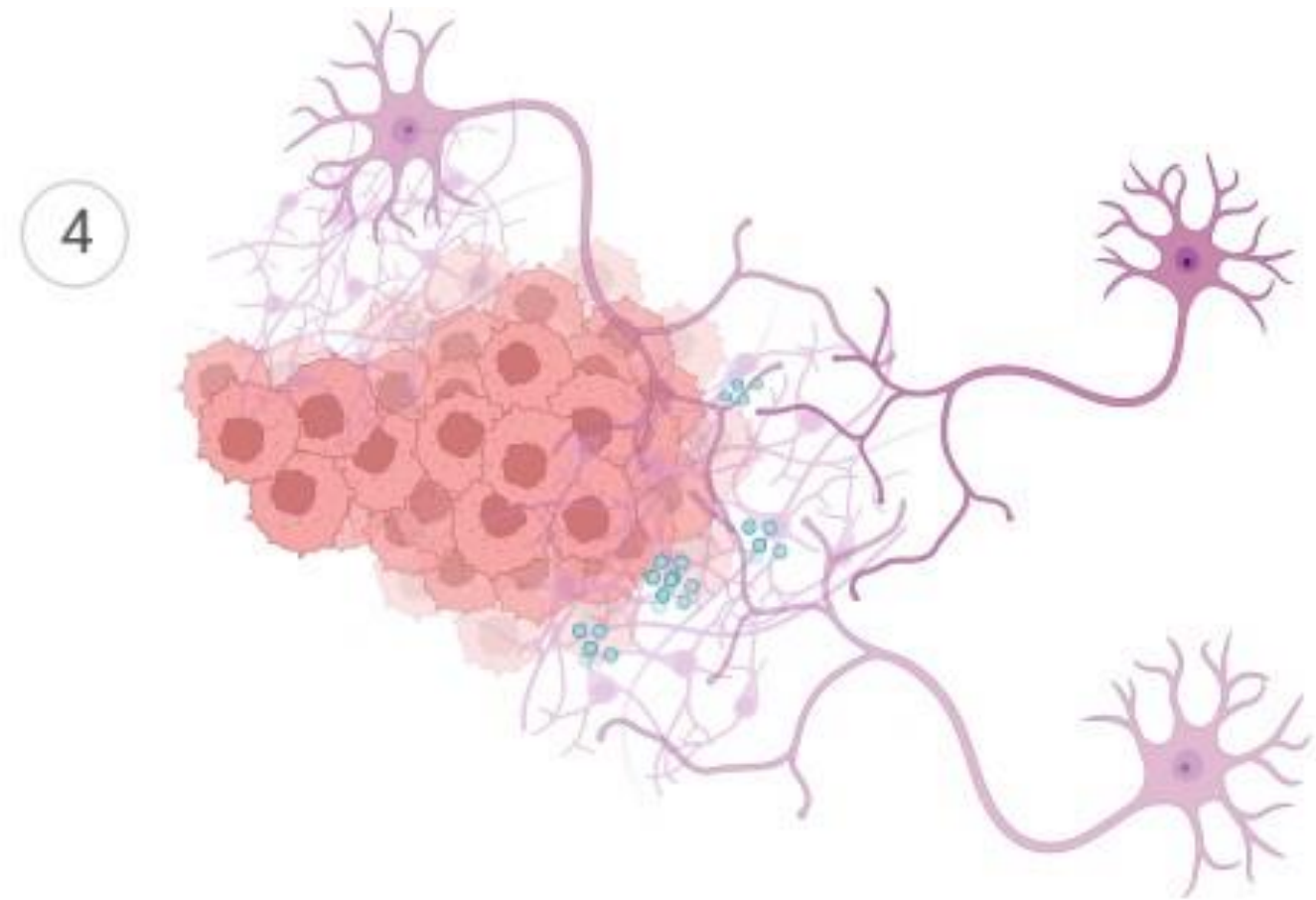


# Mechanism of Perineural Invasion

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Tumor cells detaching from the main mass and circulating the nerve whilst proliferating.



Cancer cells spread along and through nerves.

# Mathematical Model

$$\frac{dG}{dt} = s_p T_p + s_i T_i N - d_G G - \gamma_T (T_p + T_i) G - \gamma_N N G$$

$$\frac{dT_i}{dt} = \rho i (\mu_0 + \mu_1 G) T_p - d_T T_i$$

$$\frac{dT_p}{dt} = \left( r_{T_p} + \frac{G}{\tau_1 + \tau_2 G} \right) T_p - \rho i (\mu_0 + \mu_1 G) T_p - d_T T_p$$

$$\frac{dN}{dt} = v_N G N + r_N \left( 1 - \frac{N}{K_n} \right) N - d_N (T_p + T_i) N$$

## Initial Conditions

$T_p$	5000
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$T_i$	0
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$G$	0
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$N$	2.575
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# Parameters Estimation

Parameter <sup>1</sup>	Value	Units
$s_p$	$2.22 \times 10^{-3}$	$\text{pg cell}^{-1} \text{day}^{-1}$
$s_i$	$4.5 \times 10^{-2}$	$\text{pgmm}^3(\text{daycell}^2)^{-1}$
$d_G$	22.18	$\text{day}^{-1}$
$\gamma_T$	$5.57 \times 10^{-5}$	$\text{cells}^{-1} \text{day}^{-1}$
$\gamma_N$	$5 \times 10^{-2}$	$\text{cells}^{-1} \text{day}^{-1}$
$p_i$	0.05	
$\mu_0$	0.22	$\text{day}^{-1}$
$\mu_1$	0.00173	$\text{mm}^3 \text{day}^{-1} \text{pg}^{-1}$

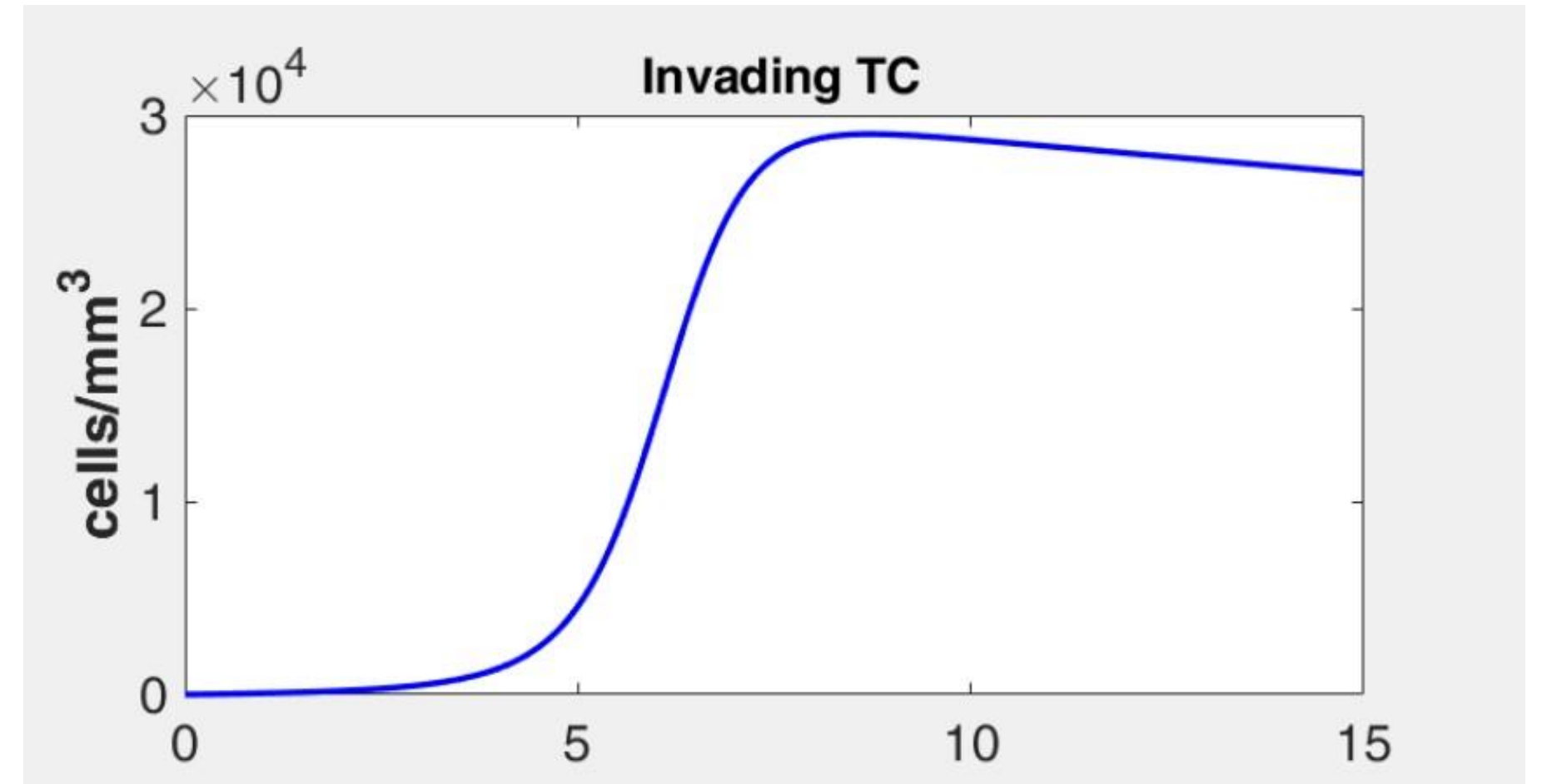
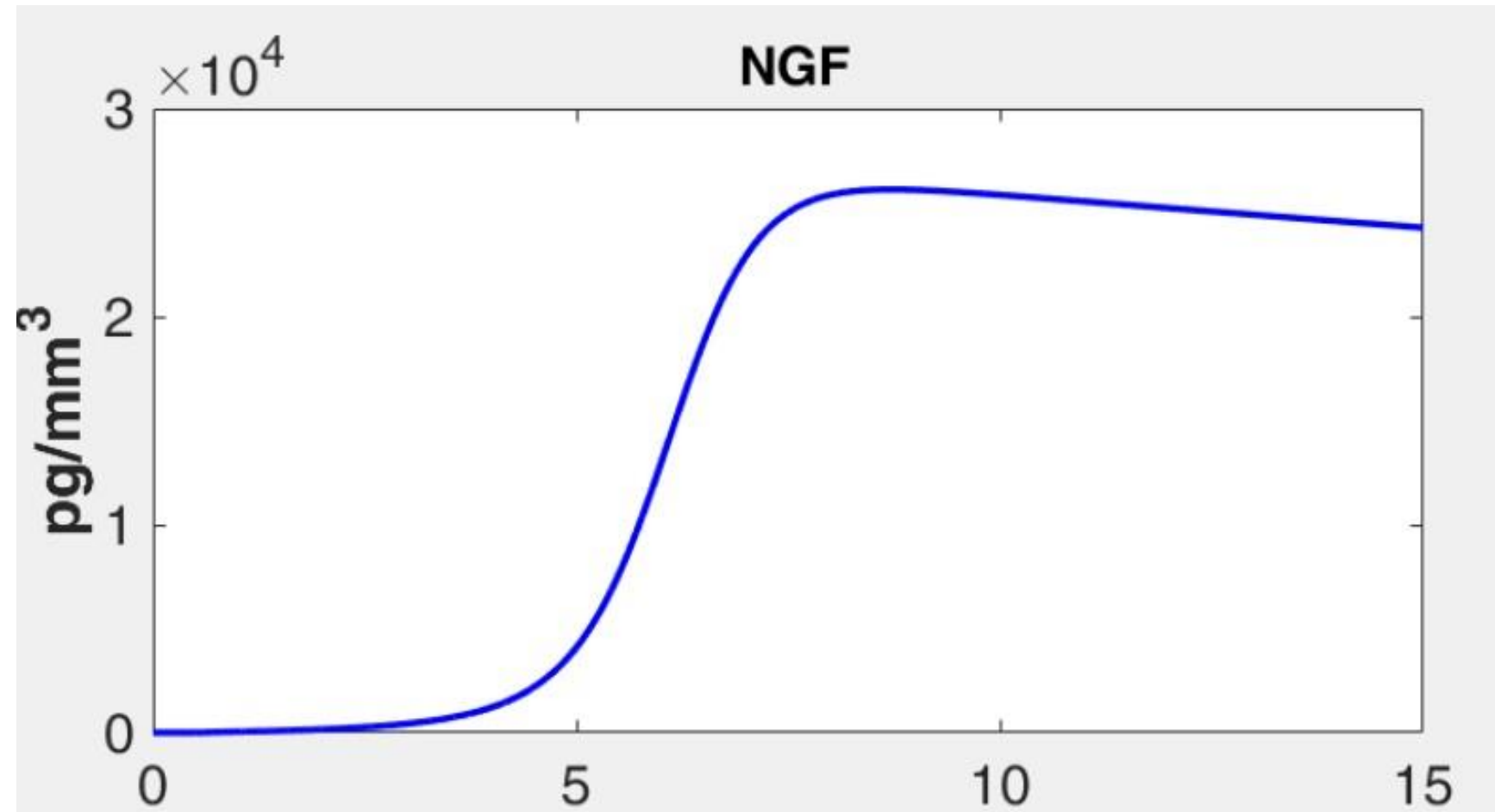
Parameter <sup>1</sup>	Value	Units
$d_T$	$1.27 \times 10^{-2}$	$\text{day}^{-1}$
$r_{Tp}$	$4.81 \times 10^{-4}$	$\text{day}^{-1}$
$\tau_1$	134.27	$\text{pgday}(\text{mm}^3)^{-1}$
$\tau_2$	2.39	day
$v_n$	10.85	$\text{pg}(\text{daymm}^3)^{-1}$
$r_n$	0.06	$\text{day}^{-1}$
$k_n$	0.26	$(\text{cells}/\text{mm}^3)^{-1}$
$d_N$	0.0000035	$(\text{cells}/\text{mm}^3)^{-1} \text{day}^{-1}$

1) Lolias, G., Bianchi, A., & Syrigos, K. N. (2016). Tumour-induced neurogenesis and perineural tumour growth: a mathematical approach. *Scientific reports*, 6(1), 1-10.



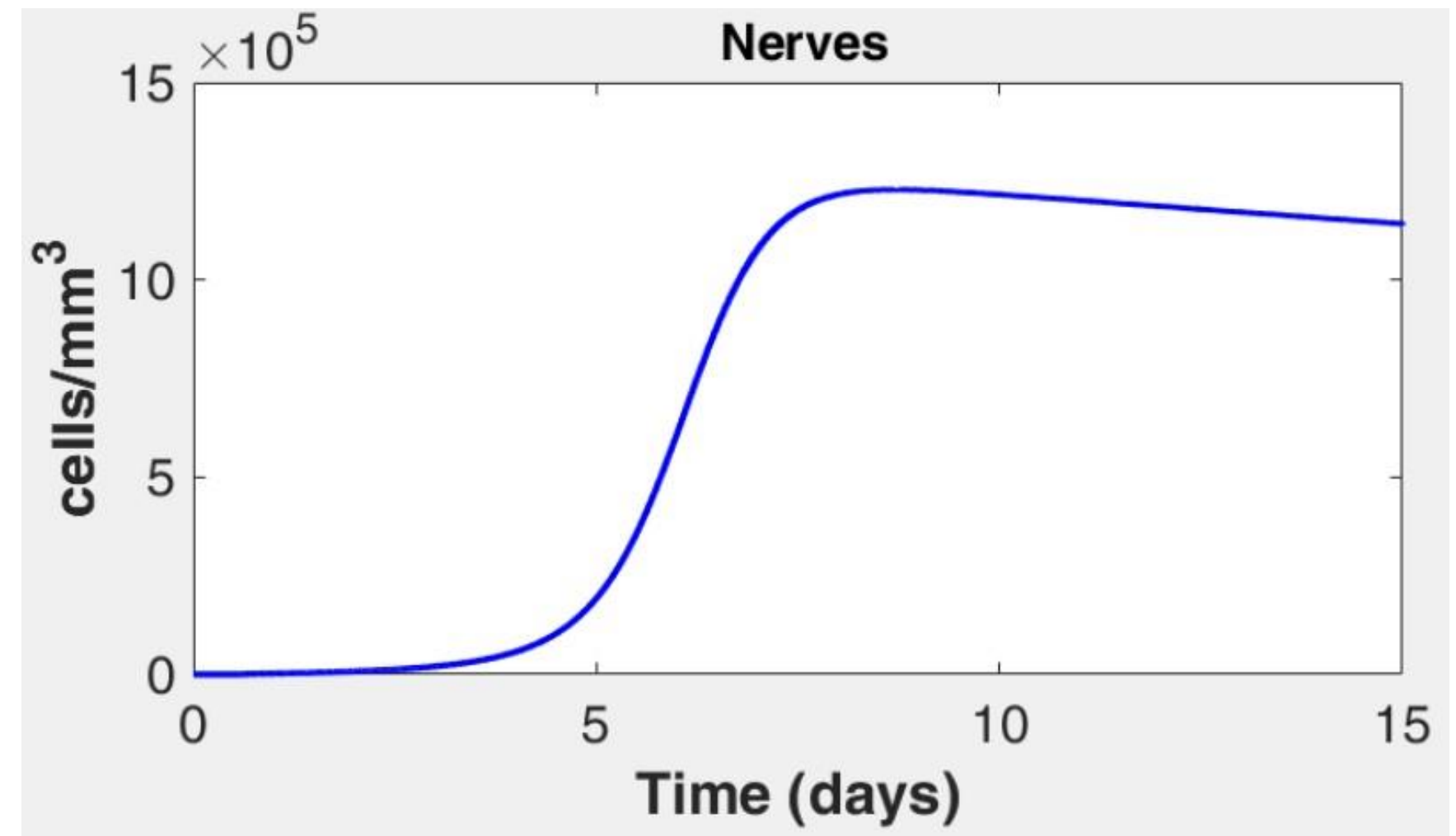
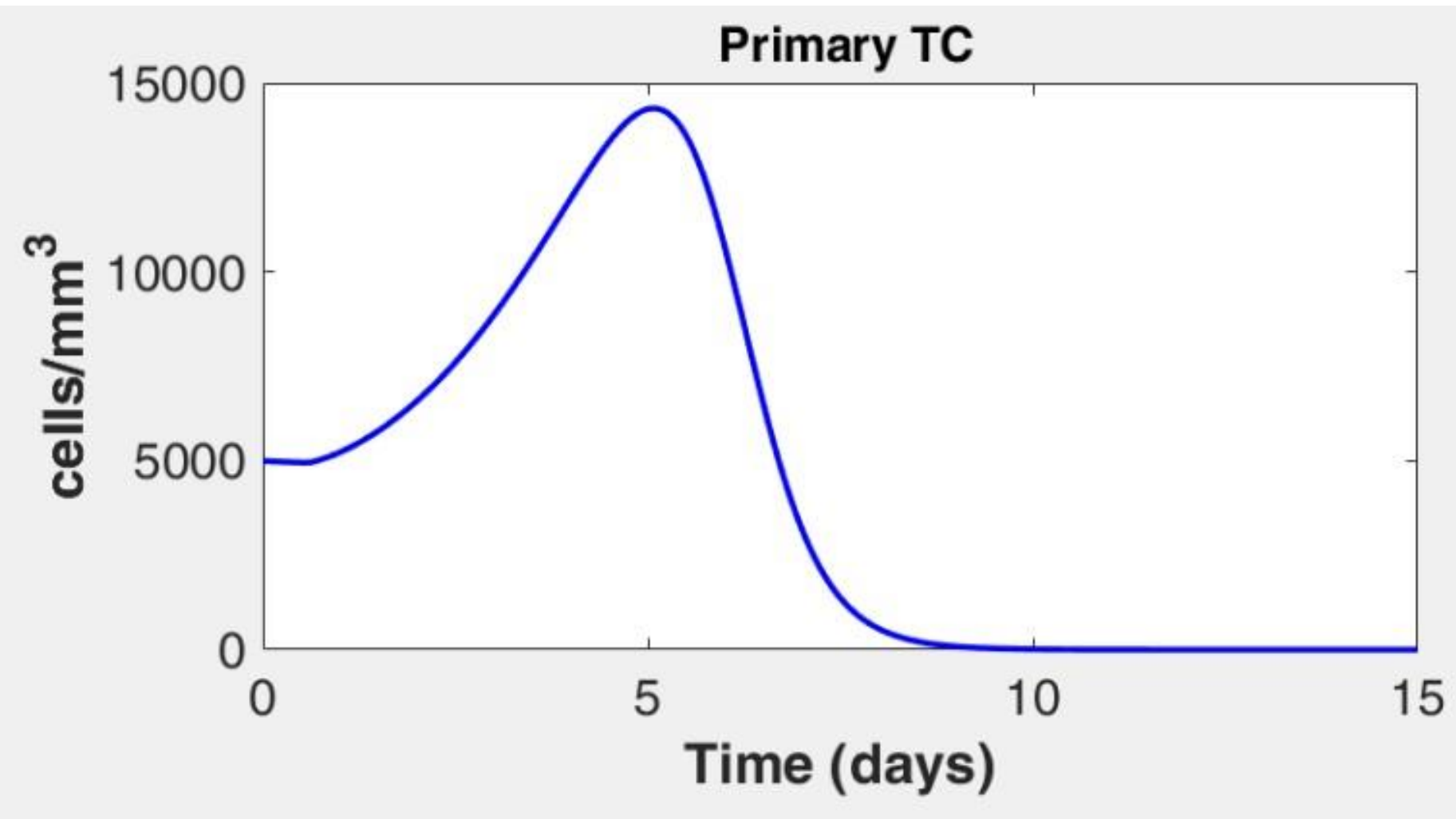
# Simulations – “go or grow” hypothesis

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Similar pattern between Invading tumor cells and Nerve growth factor as a result of the secretion of NGF by Primary tumor cells.

# Simulations – “go or grow” hypothesis



Primary tumor cells are over proliferating until day 5 (go or grow hypothesis) and then decrease due to migration. The pattern of nerves seen in the graph suggests that nerves initially increase in density in response to the presence of cancer cells (Neurogenesis). After that, the density of nerves begins to decline slightly, possibly due damage caused by the invasion of cancer cells.

# Mathematical Model - Adding Lymphatics

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$$\frac{dG}{dt} = s_p T_p + s_i T_i N - d_G G - \gamma_T (T_p + T_i) G - \gamma_N N G$$

$$\frac{dT_i}{dt} = p_i (\mu_0 + \mu_1 G) T_p - d_T T_i + \mu_2 L T_p$$

$$\frac{dT_p}{dt} = \left( r_{T_p} + \frac{G}{\tau_1 + \tau_2 G} \right) T_p - p_i (\mu_0 + \mu_1 G) T_p - d_T T_p - \mu_2 L T_p$$

$$\frac{dN}{dt} = v_N G N + r_N \left( 1 - \frac{N}{K_n} \right) N - d_N (T_p + T_i) N$$

$$\frac{dL}{dt} = r_L \left( 1 - \frac{L}{k_L} \right) + \frac{V}{\lambda_1 + \lambda_2 V} L$$

$$\frac{dV}{dt} = s_V T_p - d_V V - \gamma_V L V$$

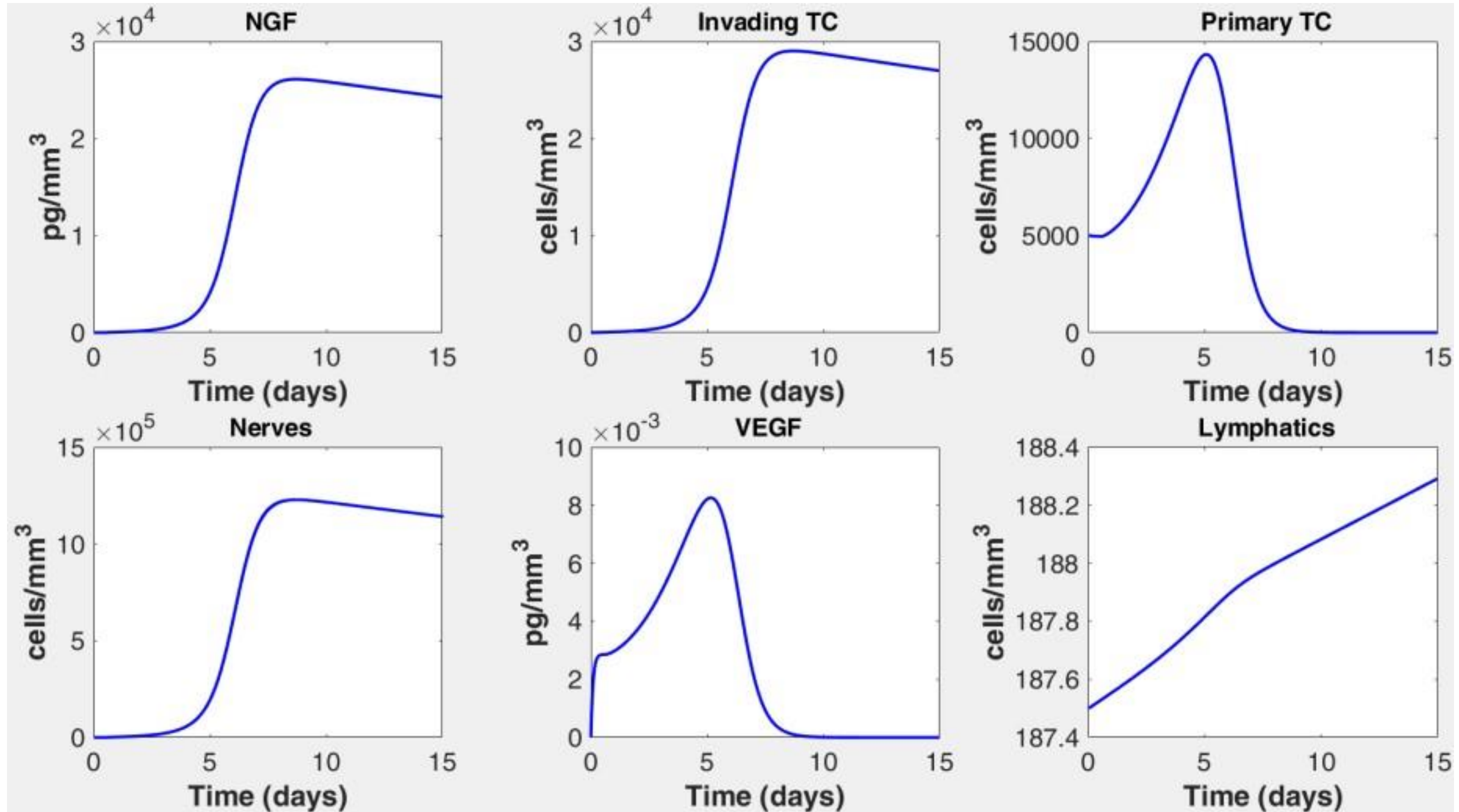
We add the term  $-\mu_2 L T_p$  to the  $T_p$  equation and  $+\mu_2 L T_p$  to the  $T_i$  equation, in order to represent tumor cells escaping the primary site through the lymphatics.

# Parameters Estimation

Parameter <sup>1</sup>	Value	Units
$s_V$	$6.5 \times 10^{-6}$	pg cell <sup>-1</sup> day <sup>-1</sup>
$d_V$	11	day <sup>-1</sup>
$\gamma_V$	$1.4 \times 10^{-3}$	mm <sup>3</sup> cells <sup>-1</sup> day <sup>-1</sup>
$r_L$	0.042	day <sup>-1</sup>
$k_L$	$18.52 \times 10^5$	cells day (mm <sup>3</sup> ) <sup>-1</sup>
$\mu_2$	$4.8 \times 10^{-8}$	cellday <sup>-1</sup>
$\lambda_1$	42	day
$\lambda_2$	4.1	pg day mm <sup>3</sup>

1) Bianchi, A., Painter, K. J., & Sherratt, J. A. (2015). A mathematical model for lymphangiogenesis in normal and diabetic wounds. *Journal of theoretical biology*, 383, 61-86.

# Results after the addition of VEGF (V) and Lymphatic Endothelial Cell (L)





# Discussion and future directions

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- We presented the first attempt of modelling tumor cells, nerves and lymphatics interactions in PNI
- We managed to capture the *go or grow* hypothesis of the tumor cells based upon the interactions with the neurons
- We will further investigate these interactions by including other tumor microenvironmental factors such as macrophages, fibroblasts etc.
- Provides a fundamental basis for further examination of the interactions that occur during perineural invasion

# Acknowledgments

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Thank you for  
your attention!